



Figura 3.76

3.10 Exercícios Propostos

3.10.1 - Simplifique cada expressão, utilizando a Álgebra de Boole.

a) $S = A\bar{B}\bar{C} + \bar{A}\bar{B}C + ABC + \bar{A}BC + \bar{A}\bar{B}\bar{C}$

b) $S = A\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D}$

3.10.2 - Simplifique utilizando a Álgebra de Boole:

$$S = \overline{[(\bar{B} + \bar{C} + \bar{D})(\bar{A} + B + C) + C]} + \bar{A}\bar{B}C + \bar{B}(\bar{A} + C)$$

3.10.3 - Idem, para a expressão:

$$S = A[\overline{B(\bar{C} + D)} + \overline{A(\bar{B} + \bar{C})}] + C\bar{D} + A\bar{B}C + AB$$

3.10.4 - Idem, para a expressão:

$$S = (\bar{A} \oplus B + \bar{B}\bar{C}\bar{D})[\bar{D} + \bar{B}C + D(\bar{A} + B)] + \bar{A}\bar{D}$$

3.10.5 - Idem, para a expressão:

$$S = \overline{[(B + \bar{C}D + D + AC)(A + \bar{B} + \bar{C}) + \bar{B}(C + \bar{A}BC + AC)](A + B)}$$

3.10.6 - Desenhe o circuito que executa a expressão, simplificado.

$$S = \overline{(\bar{B} + \bar{D})\{ \bar{B} + C \odot D + \bar{A}[\bar{B}\bar{C} + \bar{B}C + A + B(\bar{C} + \bar{D})] \}}$$

3.10.7 - Simplifique através da Álgebra de Boole:

$$S = (\overline{A}B + C\overline{D} + AD) \{ \overline{B}[C \oplus D + \overline{A}(\overline{B} + \overline{C}) + A\overline{B}\overline{C}] + \overline{A} \}$$

3.10.8 - Demonstre que:

$$A \odot (B \oplus C) = A \oplus (B \odot C)$$

3.10.9 - Através dos diagramas de Veitch-Karnaugh, determine a expressão simplificada de S_1 e S_2 da tabela 3.26.

A B	S_1	S_2
0 0	1	1
0 1	0	1
1 0	1	0
1 1	1	0

Tabela 3.26

3.10.10 - Simplifique as expressões de S_1 , S_2 , S_3 e S_4 da tabela 3.27, utilizando os mapas de Veitch-Karnaugh.

A	B	C	S_1	S_2	S_3	S_4
0	0	0	1	1	0	0
0	0	1	0	1	1	1
0	1	0	1	1	0	1
0	1	1	1	0	0	0
1	0	0	1	1	1	1
1	0	1	1	1	1	0
1	1	0	0	1	1	1
1	1	1	1	0	0	1

Tabela 3.27

3.10.11 - Idem ao anterior, para a tabela 3.28.

A	B	C	D	S ₁	S ₂	S ₃	S ₄
0	0	0	0	1	1	0	0
0	0	0	1	1	0	0	0
0	0	1	0	1	1	1	0
0	0	1	1	1	0	0	1
0	1	0	0	1	1	1	1
0	1	0	1	0	1	1	1
0	1	1	0	0	1	1	0
0	1	1	1	1	1	0	1
1	0	0	0	1	1	0	0
1	0	0	1	1	1	0	1
1	0	1	0	1	0	1	0
1	0	1	1	1	0	0	0
1	1	0	0	1	0	0	0
1	1	0	1	0	1	1	1
1	1	1	0	0	0	0	1
1	1	1	1	1	1	0	1

Tabela 3.28

3.10.12- Simplifique as expressões utilizando diagramas de Veitch-Karnaugh:

a) $S = A\overline{B}\overline{C} + A\overline{B}C + \overline{A}BC + \overline{A}\overline{B}\overline{C} + ABC$

b) $S = \overline{A}BC\overline{D} + \overline{A}BCD + \overline{A}\overline{B}\overline{C}\overline{D} + AB\overline{C}\overline{D} + \overline{A}BCD + \overline{A}\overline{B}\overline{C}D + ABCD + \overline{A}\overline{B}\overline{C}D$

c) $S = \overline{B}\overline{D} + \overline{A} + A\overline{B}\overline{C}D + \overline{A}\overline{B}CD + \overline{A}\overline{C}$

d) $S = ABC + AB + \overline{A}BCD + BD + CD + \overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}\overline{C}\overline{D}$

3.10.13 - Determine as expressões simplificadas para S₁ e S₂ da tabela 3.29.

A	B	C	D	E	S ₁	S ₂
0	0	0	0	0	1	1
0	0	0	0	1	1	0
0	0	0	1	0	1	1
0	0	0	1	1	1	0
0	0	1	0	0	0	1
0	0	1	0	1	1	1
0	0	1	1	0	0	1
0	0	1	1	1	1	1
0	1	0	0	0	0	1
0	1	0	0	1	0	0
0	1	0	1	0	1	1
0	1	0	1	1	0	0
0	1	1	0	0	1	1
0	1	1	0	1	1	1
0	1	1	1	0	0	1
0	1	1	1	1	1	1
1	0	0	0	0	1	1
1	0	0	0	1	1	0
1	0	0	1	0	0	1
1	0	0	1	1	0	1
1	0	1	0	0	0	1
1	0	1	0	1	1	1
1	0	1	1	0	0	1
1	0	1	1	1	1	1
1	1	0	0	0	0	1

Tabela 3.29 (parte)

A	B	C	D	E	S ₁	S ₂
1	1	0	0	1	0	0
1	1	0	1	0	1	1
1	1	0	1	1	0	0
1	1	1	0	0	0	1
1	1	1	0	1	1	1
1	1	1	1	0	0	1
1	1	1	1	1	1	1

Tabela 3.29

3.10.14 - Simplifique as expressões de S₁ e S₂ da tabela 3.30.

A	B	C	S ₁	S ₂
0	0	0	X	1
0	0	1	0	X
0	1	0	1	0
0	1	1	X	0
1	0	0	1	0
1	0	1	X	1
1	1	0	X	X
1	1	1	1	X

Tabela 3.30

3.10.15 - Determine as expressões simplificadas de S₁, S₂, S₃ e S₄ da tabela 3.31.

A	B	C	D	S ₁	S ₂	S ₃	S ₄
0	0	0	0	1	X	0	X
0	0	0	1	X	X	0	0
0	0	1	0	X	1	0	X
0	0	1	1	X	0	1	1
0	1	0	0	1	X	X	1
0	1	0	1	0	1	X	X
0	1	1	0	X	0	1	0
0	1	1	1	X	1	0	1
1	0	0	0	X	1	X	0
1	0	0	1	1	0	1	1
1	0	1	0	X	X	0	0
1	0	1	1	1	1	0	X
1	1	0	0	X	0	1	1
1	1	0	1	X	1	0	1
1	1	1	0	1	1	X	1
1	1	1	1	0	X	1	X

Tabela 3.31

3.10.16 - Desenhe os circuitos minimizados que executam as saídas S₁ e S₂ da tabela da verdade:

A	B	C	D	E	S ₁	S ₂
0	0	0	0	0	0	1
0	0	0	0	1	0	X
0	0	0	1	0	1	1
0	0	0	1	1	0	X
0	0	1	0	0	1	X
0	0	1	0	1	1	1
0	0	1	1	0	0	X
0	0	1	1	1	1	1
0	1	0	0	0	0	1
0	1	0	0	1	0	0
0	1	0	1	0	1	1
0	1	0	1	1	0	0
0	1	1	0	0	1	X
0	1	1	0	1	1	1
0	1	1	1	0	0	0
0	1	1	1	1	1	1
1	0	0	0	0	0	1
1	0	0	0	1	0	X
1	0	0	1	0	1	1
1	0	0	1	1	0	0
1	0	1	0	0	1	X
1	0	1	0	1	1	1
1	0	1	1	0	0	0
1	0	1	1	1	1	1
1	1	0	0	0	0	X
1	1	0	0	1	0	1
1	1	0	1	0	1	1
1	1	0	1	1	0	1
1	1	1	0	0	1	1
1	1	1	0	1	1	X
1	1	1	1	0	0	1
1	1	1	1	1	1	X

Tabela 3.32

3.10.17 - Obtenha a expressão simplificada:

$$S = (\bar{A} + B) (\bar{B} + (B \oplus C) [\bar{A} \bar{B} C + B(A + \bar{D}) + \bar{B} C + \bar{B} D] + A \bar{B} D)$$

3.10.18 - Prove que:

$$\bar{A} \oplus B \oplus C \oplus D = A \oplus B \oplus C \oplus D$$